

Planning



Components of a Planning System



- In any general problem solving systems, elementary techniques to perform following functions are required
 - Choose the best rule (based on heuristics) to be applied
 - Apply the chosen rule to get new problem state
 - Detect when a solution has been found
 - Detect dead ends so that new directions are explored.

Advanced Problem Solving Approaches



- In order to solve nontrivial problems, it is necessary to combine
 - Basic problem solving strategies
 - Knowledge representation mechanisms
 - Partial solutions and at the end combine into complete problem solution (decomposition)
- Planning refers to the process of computing several steps of a problem solving before executing any of them.
- Planning is useful as a problem solving technique for non decomposable problem.



Choose Rules to apply

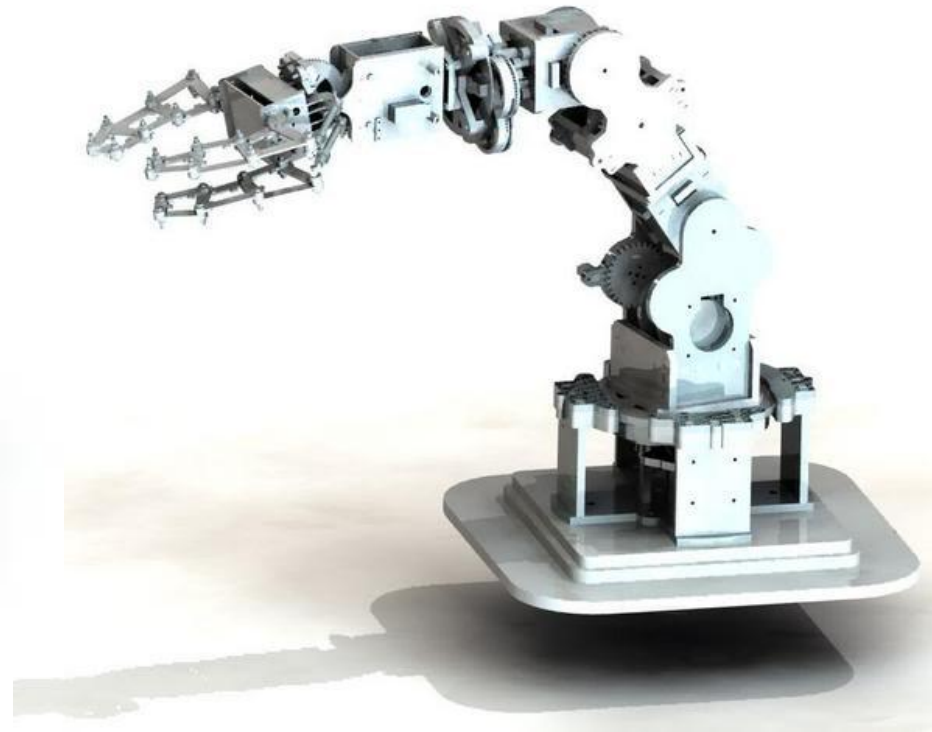
- Most widely used technique for selecting appropriate rules is to
 - first isolate a set of differences between the desired goal state and current state,
 - identify those rules that are relevant to reducing these difference,
 - if more rules are found then apply heuristic information to choose out of them.



Apply Rules

- In simple problem solving system, applying rules was easy as each rule specifies the problem state that would result from its application.
- In complex problem we deal with rules that specify only a small part of the complete problem state.

Block World Problem



Example: Block World Problem



- Block world problem assumptions
 - Square blocks of same size
 - Blocks can be stacked one upon another.
 - Flat surface (table) on which blocks can be placed.
 - Robot arm that can manipulate the blocks. It can hold only one block at a time.
- In block world problem, the state is described by a set of predicates representing the facts that were true in that state.
- One must describe for every action, each of the changes it makes to the state description.
- In addition, some statements that everything else remains unchanged is also necessary.

Actions (Operations) done by Robo



- UNSTACK (X, Y) : **[US (X, Y)]**
 - Pick up X from its current position on block Y. The arm must be empty and X has no block on top of it.
- STACK (X, Y): **[S (X, Y)]**
 - Place block X on block Y. Arm must holding X and the top of Y is clear.
- PICKUP (X): **[PU (X)]**
 - Pick up X from the table and hold it. Initially the arm must be empty and top of X is clear.
- PUTDOWN (X): **[PD (X)]**
 - Put block X down on the table. The arm must have been holding block X.



- Predicates used to describe the state
 - ON(X, Y) - Block X on block Y.
 - ONT(X) - Block X on the table.
 - CL(X) - Top of X clear.
 - HOLD(X) - Robot-Arm holding X.
 - AE - Robot-arm empty.
- Logical statements true in this block world.
 - Holding X means, arm is not empty
 $(\exists X) \text{ HOLD } (X) \rightarrow \sim \text{AE}$
 - X is on a table means that X is not on the top of any block
 $(\forall X) \text{ ONT } (X) \rightarrow \sim (\exists Y) \text{ ON } (X, Y)$
 - Any block with no block on has clear top
 $(\forall X) (\sim (\exists Y) \text{ ON } (Y, X)) \rightarrow \text{CL } (X)$

Effect of Unstack operation



- The effect of $US(X, Y)$ is described by the following axiom
$$[CL(X, State) \wedge ON(X, Y, State)] \rightarrow [HOLD(X, DO(US(X, Y), State)) \wedge CL(Y, DO(US(X, Y), State))]$$
 - DO is a function that generates a new state as a result of given action and a state.
- For each operator, set of rules (called frame axioms) are defined where the components of the state are
 - affected by an operator
 - If $US(A, B)$ is executed in state S_0 , then we can infer that $HOLD(A, S_1) \wedge CLEAR(B, S_1)$ holds true, where S_1 is new state after Unstack operation is executed.
 - not affected by an operator
 - If $US(A, B)$ is executed in state S_0 , B in S_1 is still on the table but we can't derive it. So frame rule stating this fact is defined as $ONT(Z, S) \rightarrow ONT(Z, DO(US(A, B), S))$



- Advantage of this approach is that
 - simple mechanism of resolution can perform all the operations that are required on the state descriptions.
- Disadvantage is that
 - number of axioms becomes very large for complex problem such as COLOR of block also does not change.
 - So we have to specify rule for each attribute.
$$\text{COLOR}(X, \text{red}, S) \rightarrow \text{COLOR}(X, \text{red}, \text{DO}(\text{US}(Y, Z), s))$$
- To handle complex problem domain, there is a need of mechanism that does not require large number of explicit frame axioms.

STRIPS Mechanism

- One such mechanism was used in early robot problem solving system named STRIPS (developed by Fikes, 1971).
- In this approach, each operation is described by three lists.
 - **Pre_Cond list** contains predicates which have to be true before operation.
 - **ADD list** contains those predicates which will be true after operation
 - **DELETE list** contain those predicates which are no longer true after operation
- Predicates not included on either of these lists are assumed to be unaffected by the operation.
- Frame axioms are specified implicitly in STRIPS which greatly reduces amount of information stored.



STRIPS – Style Operators

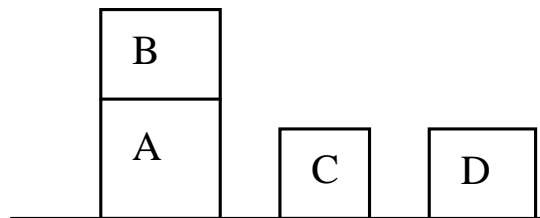
- S (X, Y)
 - Pre: $CL(Y) \wedge HOLD(X)$
 - Del: $CL(Y) \wedge HOLD(X)$
 - Add: $AE \wedge ON(X, Y)$
- US (X, Y)
 - Pre: $ON(X, Y) \wedge CL(X) \wedge AE$
 - Del: $ON(X, Y) \wedge AE$
 - Add: $HOLD(X) \wedge CL(Y)$
- PU (X)
 - Pre: $ONT(X) \wedge CL(X) \wedge AE$
 - Del: $ONT(X) \wedge AE$
 - Add: $HOLD(X)$
- PD (X)
 - Pre: $HOLD(X)$
 - Del: $HOLD(X)$
 - Add: $ONT(X) \wedge AE$

Goal stack method - Example

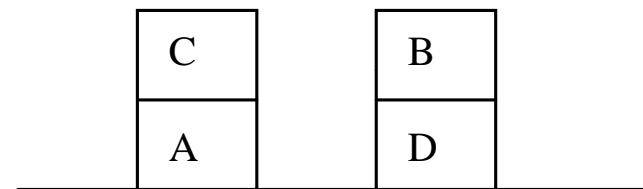


- Logical representation of Initial and Goal states:
 - Initial State: $ON(B, A) \wedge ONT(C) \wedge ONT(A) \wedge ONT(D) \wedge CL(B) \wedge CL(C) \wedge CL(D) \wedge AE$
 - Goal State: $ON(C, A) \wedge ON(B, D) \wedge ONT(A) \wedge ONT(D) \wedge CL(C) \wedge CL(B) \wedge AE$

Initial State



Goal State





- We notice that following sub-goals in goal state are also true in initial state.

$$\text{ONT}(A) \wedge \text{ONT}(D) \wedge \text{CL}(C) \wedge \text{CL}(B) \wedge \text{AE}$$

- Represent for the sake of simplicity - **TSUBG**.
- Only sub-goals $\text{ON}(C, A)$ & $\text{ON}(B, D)$ are to be satisfied and finally make sure that **TSUBG** remains true.
- Either start solving first $\text{ON}(C, A)$ or $\text{ON}(B, D)$. Let us solve first $\text{ON}(C, A)$.

Goal Stack:

$\text{ON}(C, A)$

$\text{ON}(B, D)$

$\text{ON}(C, A) \wedge \text{ON}(B, D) \wedge \text{TSUBG}$



- To solve $ON(C, A)$, operation $S(C, A)$ could only be applied.
- So replace $ON(C, A)$ with $S(C, A)$ in goal stack.

Goal Stack:

$S(C, A)$

$ON(B, D)$

$ON(C, A) \wedge ON(B, D) \wedge TSUBG$

- $S(C, A)$ can be applied if its preconditions are true. So add its preconditions on the stack.

Goal Stack:

$CL(A)$

$HOLD(C)$ Preconditions of STACK

$CL(A) \wedge HOLD(C)$

$S(C, A)$ Operator

$ON(B, D)$

$ON(C, A) \wedge ON(B, D) \wedge TSUBG$

- Next check if $CL(A)$ is true in $State_0$.
- Since it is not true in $State_0$, only operator that could make it true is $US(B, A)$.
- So replace $CL(A)$ with $US(B, A)$ and add its preconditions.

Goal Stack: $ON(B, A)$

$CL(B)$ Preconditions of UNSTACK

AE

$ON(B, A) \wedge CL(B) \wedge AE$

$US(B, A)$ Operator

$HOLD(C)$

$CL(A) \wedge HOLD(C)$

$S(C, A)$ Operator

$ON(B, D)$

$ON(C, A) \wedge ON(B, D) \wedge TSUBG$



- $ON(B, A)$, $CL(B)$ and AE are all true in initial state, so pop these all from its compound goal.
- Next pop top operator $US(B, A)$ and produce new state by using its ADD and $DELETE$ lists.
- Add $US(B, A)$ in a queue of sequence of operators.

SQUEUE = US (B, A)

State_1:

$ONT(A) \wedge ONT(C) \wedge ONT(D) \wedge HOLD(B) \wedge CL(A) \wedge CL(C) \wedge CL(D)$

Goal Stack:

HOLD(C)

$CL(A) \wedge HOLD(C)$

S (C, A)

Operator

$ON(B, D)$

$ON(C, A) \wedge ON(B, D) \wedge TSUBG$



- To satisfy the goal $HOLD(C)$, two operators can be used e.g., $PU(C)$ or $US(C, X)$, where X could be any block. Let us choose $PU(C)$ and proceed further.
- Repeat the process. Change in states is shown below.

State_1:

$ONT(A) \wedge ONT(C) \wedge ONT(D) \wedge HOLD(B) \wedge ACL(A) \wedge CL(C) \wedge ACL(D)$
SQUEUE = US (B, A)

- Next operator to be popped of is $S(B, D)$. So

State_2:

$ONT(A) \wedge ONT(C) \wedge ONT(D) \wedge ON(B, D) \wedge ACL(A) \wedge CL(C) \wedge ACL(B) \wedge AE$
SQUEUE = US (B, A), S(B, D)

State_3:

$ONT(A) \wedge HOLD(C) \wedge ONT(D) \wedge ON(B, D) \wedge ACL(A) \wedge ACL(B)$
SQUEUE = US (B, A), S(B, D), PU(C)

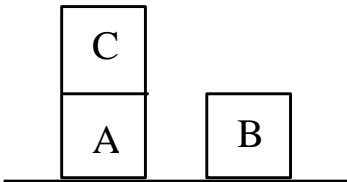
State_4:

$ONT(A) \wedge ON(C, A) \wedge ONT(D) \wedge ON(B, D) \wedge ACL(C) \wedge ACL(B) \wedge AE$
SQUEUE = US (B, A), S(B, D), PU(C), S(C, A)

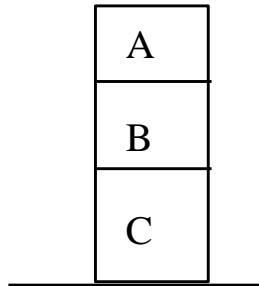


Example 2

Initial State (State0)



Goal State

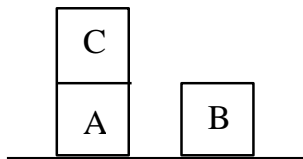




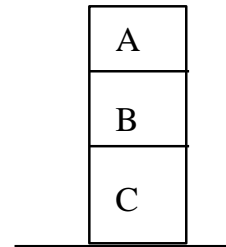
Example 2

- The Goal stack method is not efficient for difficult problems such as Sussman anomaly problem.
- It fails to find good solution.
- Let us consider the Sussman anomaly problem

Initial State (State0)



Goal State



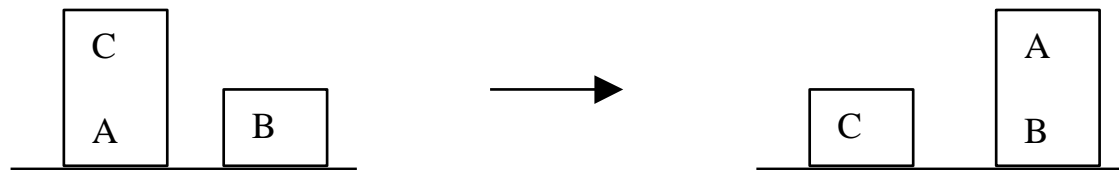


Initial State: $ON(C, A) \wedge ONT(A) \wedge ONT(B)$

Goal State: $ON(A, B) \wedge ON(B, C)$

- Remove CL and AE predicates for the sake of simplicity.
- To satisfy $ON(A, B)$, following operators are applied

US(C, A) , PD(C), PU(A) and S(A, B)



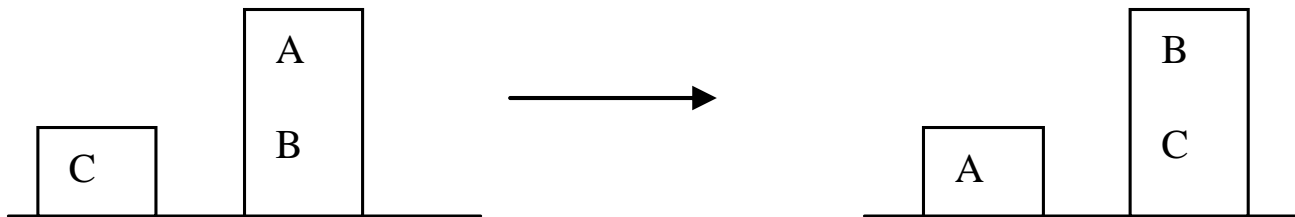


State_1: $ON(B, A) \wedge ONT(C)$

- To satisfy $ON(B, C)$, following operators are applied

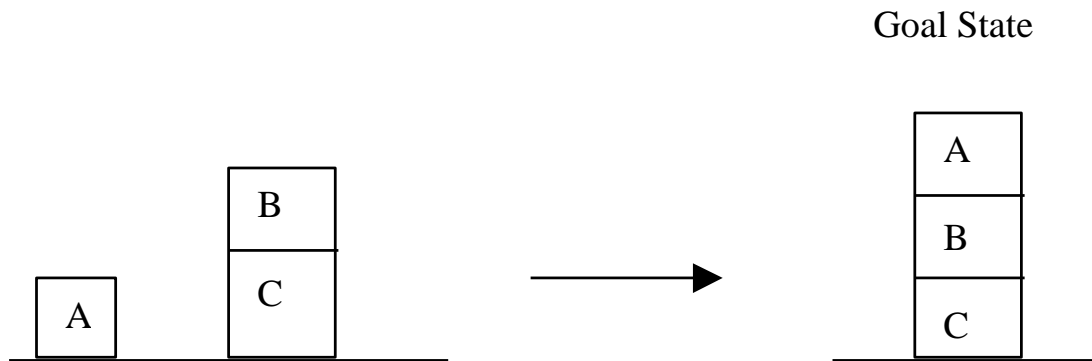
US(A, B), PD(A), PU(B) and S(B, C)

State_2: $ON(B, C) \wedge ONT(A)$





- Finally satisfy combined goal $ON(A, B) \wedge ON(B, C)$.
- Combined goal fails as while satisfying $ON(B, C)$, we have undone $ON(A, B)$.
- Difference in goal and current state is $ON(A, B)$.
- Operations required are $PU(A)$ and $S(A, B)$





Solution

- The complete plan for solution is as follows:
 1. US(C, A)
 2. PD (C)
 3. **PU(A)**
 4. **S(A, B)**
 5. **US(A, B)**
 6. **PD(A)**
 7. PU(B)
 8. S(B, C)
 9. PU(A)
 10. S(A, B)
- Although this plan will achieve the desired goal, but it is not efficient.



- In order to get efficient plan, either repair this plan or use some other method.
- Repairing is done by looking at places where operations are done and undone immediately, such as $S(A, B)$ and $US(A, B)$.
- By removing them, we get
 1. $US(C, A)$
 2. $PD(C)$
 3. $PU(B)$
 4. $S(B, C)$
 5. $PU(A)$
 6. $S(A, B)$

Planning vs. Problem Solving



- Planning and problem solving (Search) are considered **as different approaches** even though they can often be applied to the same problem.
- Basic problem solving searches a state-space of possible actions, starting from an initial state and following **any path that it believes will lead it the goal state.**
- Planning is distinct from this in three key ways:
 1. **Planning “opens up” the representation of states, goals and actions** so that the planner can deduce direct connections between states and actions.
 2. The **planner does not have to solve the problem** in order (from initial to goal state) it can suggest actions to solve any sub-goals at anytime.
 3. Planners assume that most parts of the world **are independent** so they can be stripped apart and solved individually.



Finding a solution

1. Look at the state of the world:
 - Is it the goal state? If so, the list of operators so far is the plan to be applied.
 - If not, go to Step 2.

2. Pick an operator:
 - Check that it has not already been applied (to stop looping).
 - Check that the preconditions are satisfied.

If either of these checks fails, backtrack to get another operator.

3. Apply the operator:
 1. Make changes to the world: delete from and add to the world state.
 2. Add operator to the list of operators already applied.
 3. Go to Step 1.



STRIPS Representation

- Planning can be considered as a logical inference problem:
 - a plan is inferred from facts and logical relationships.
- STRIPS represented planning problems as a series of state descriptions and operators expressed in first-order predicate logic.

represent the state of the world at three points during the plan:

- Initial state, the state of the world at the start of the problem;
- Current state, and
- Goal state, the state of the world we want to get to.

Operators are actions that can be applied to change the state of the world.

- Each operator has outcomes i.e. how it affects the world.
- Each operator can only be applied in certain circumstances. These are the preconditions of the operator.

Representing Operators



- STRIPS operators are defined as:
 - **NAME:** How we refer to the operator e.g. go(Agent, From, To).
 - **PRECONDITIONS:** What states need to hold for the operator to be applied. e.g. [at(Agent, From)].
 - **ADD LIST:** What new states are added to the world as a result of applying the operator e.g. [at(Agent, To)].
 - **DELETE LIST:** What old states are removed from the world as a result of applying the operator. e.g. [at(Agent, From)].